

P27.2 $\lambda = \frac{v}{f} = \frac{354 \text{ m/s}}{2000 \text{ s}^{-1}} = 0.177 \text{ m}$

(a) $d \sin \theta = m\lambda$ so $(0.300 \text{ m}) \sin \theta = 1(0.177 \text{ m})$ and $\theta = \boxed{36.2^\circ}$

(b) $d \sin \theta = m\lambda$ so $d \sin 36.2^\circ = 1(0.0300 \text{ m})$ and $d = \boxed{5.08 \text{ cm}}$

(c) $(1.00 \times 10^{-6} \text{ m}) \sin 36.2^\circ = (1)\lambda$ so $\lambda = 590 \text{ nm}$

$$f = \frac{c}{\lambda} = \frac{3.00 \times 10^8 \text{ m/s}}{5.90 \times 10^{-7} \text{ m}} = \boxed{508 \text{ THz}}$$

- P27.15 (a) The light reflected from the top of the oil film undergoes phase reversal. Since $1.45 > 1.33$, the light reflected from the bottom undergoes no reversal. For constructive interference of reflected light, we then have

$$2nt = \left(m + \frac{1}{2}\right)\lambda$$

or $\lambda_m = \frac{2nt}{m + (1/2)} = \frac{2(1.45)(280 \text{ nm})}{m + (1/2)}$.

Substituting for m gives: $m = 0$, $\lambda_0 = 1620 \text{ nm}$ (infrared)

$m = 1$, $\lambda_1 = 541 \text{ nm}$ (green)

$m = 2$, $\lambda_2 = 325 \text{ nm}$ (ultraviolet).

Both infrared and ultraviolet light are invisible to the human eye, so the dominant color in reflected light is green.

- (b) The dominant wavelengths in the transmitted light are those that produce destructive interference in the reflected light. The condition for destructive interference upon reflection is

$$2nt = m\lambda$$

or $\lambda_m = \frac{2nt}{m} = \frac{812 \text{ nm}}{m}$.

Substituting for m gives: $m = 1$, $\lambda_1 = 812 \text{ nm}$ (near infrared)

$m = 2$, $\lambda_2 = 406 \text{ nm}$ (violet)

$m = 3$, $\lambda_3 = 271 \text{ nm}$ (ultraviolet).

Of these, the only wavelength visible to the human eye (and hence the dominate wavelength observed in the transmitted light) is 406 nm. Thus, the dominant color in the transmitted light is violet.

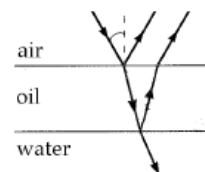


FIG. P27.15

P27.21 $\frac{y}{L} \approx \sin \theta = \frac{m\lambda}{a}$ $\Delta y = 3.00 \times 10^{-3} \text{ nm}$

$\Delta m = 3 - 1 = 2$ and $a = \frac{\Delta m \lambda L}{\Delta y}$

$$a = \frac{2(690 \times 10^{-9} \text{ m})(0.500 \text{ m})}{(3.00 \times 10^{-3} \text{ m})} = \boxed{2.30 \times 10^{-4} \text{ m}}$$

- P27.46 The central bright fringe is wider than the side bright fringes, so the light must have been diffracted by a single slit. For precision, we measure to the third minimum from the center

$$\begin{aligned}
 y &= 4.0 \text{ cm} \\
 \tan \theta &= \frac{y}{L} = \frac{0.04 \text{ m}}{2.6 \text{ m}} = 0.0154 \\
 \theta &= 0.881^\circ = 0.0154 \text{ rad} \\
 a \sin \theta &= m\lambda \\
 a &= \frac{m\lambda}{\sin \theta} = \frac{3(632.8 \times 10^{-9} \text{ m})}{\sin 0.881^\circ} = \frac{3(632.8 \times 10^{-9} \text{ m})}{0.0154} = \boxed{1.23 \times 10^{-4} \text{ m}}
 \end{aligned}$$

- P27.47 For destructive interference, the path length must differ by $m\lambda$. We may treat this problem as a double slit experiment if we remember the light undergoes a $\frac{\pi}{2}$ -phase shift at the mirror. The second slit is the mirror image of the source, 1.00 cm below the mirror plane. Modifying the equation for Young's experiment, $\frac{dy}{L} = m\lambda$ we have

$$y_{\text{dark}} = \frac{m\lambda L}{d} = \frac{1(5.00 \times 10^{-7} \text{ m})(100 \text{ m})}{(2.00 \times 10^{-2} \text{ m})} = \boxed{2.50 \text{ mm}}.$$